

Chapter 3 Study Guide-R

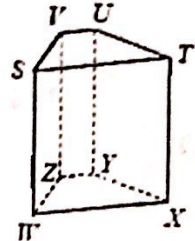
(Parallel and Perpendicular Lines)

Name Key
Date _____ Period _____

Topic 1: parallel Lines & Planes

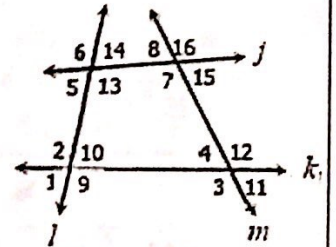
Use the diagram to the right for questions 1-5.

- Name a plane parallel to plane WXT . VUY
- Name two segments parallel to \overline{VU} . $\overline{ZY}, \overline{WX}, \overline{ST}$
- Name two segments parallel to \overline{SW} . $\overline{VZ}, \overline{UY}, \overline{TX}$
- Name two segments skew to \overline{XY} . $\overline{SV}, \overline{VU}, \overline{ST}, \overline{VZ}, \overline{SW}$
- Name two segments skew to \overline{VZ} . $\overline{VT}, \overline{YX}, \overline{ST}, \overline{WX}$



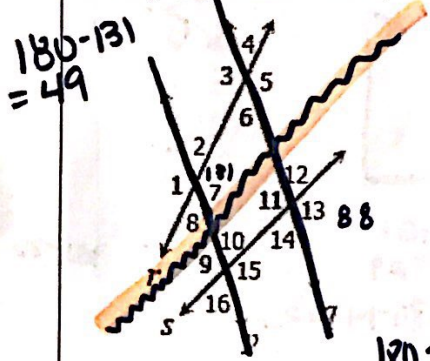
Name each angle pair as corresponding, alternate interior, alternate exterior, same side interior, or no relationship. Identify the transversal that connects each angle pair.

- $\angle 4$ and $\angle 10$ SSI; Transversal: line k
- $\angle 8$ and $\angle 11$ alt. ext; Transversal: line m
- $\angle 2$ and $\angle 12$ none (same side ext); Transversal: line k
- $\angle 5$ and $\angle 7$ Corresponding; Transversal: line j
- $\angle 2$ and $\angle 13$ alt. int; Transversal: line l



Topic 2: Parallel Lines & Angles

11. If $p \parallel q$, $m\angle 7 = 131^\circ$, and $m\angle 13 = 88^\circ$, find the measure of each missing angle.

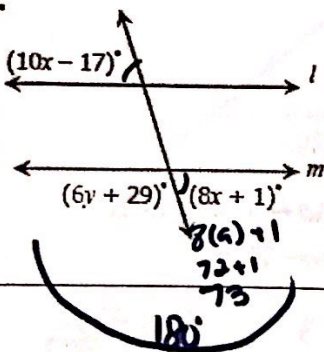


a. $m\angle 1 = 131$	b. $m\angle 6 = 49$	c. $m\angle 12 = 92$
d. $m\angle 2 = 49$	e. $m\angle 8 = 49$	f. $m\angle 14 = 92$
g. $m\angle 3 = 131$	h. $m\angle 9 = 88$	i. $m\angle 15 = 88$
j. $m\angle 4 = 49$	k. $m\angle 10 = 92$	l. $m\angle 16 = 92$
m. $m\angle 5 = 131$	n. $m\angle 11 = 88$	

$180 - 88 = 92$

For questions 12-14, find the value of x and y if $l \parallel m$.

12.



$$\begin{aligned} 10x - 17 &= 8x + 1 \\ -8x &\quad -8x \\ \hline 2x - 17 &= 1 \\ +17 &\quad +17 \\ \hline 2x &= 18 \\ \frac{2x}{2} &= \frac{18}{2} \\ x &= 9 \end{aligned}$$

$$\begin{aligned} 6y + 29 + 73 &= 180 \\ 6y + 102 &= 180 \\ -102 &\quad -102 \\ \hline 6y &= 78 \\ \frac{6y}{6} &= \frac{78}{6} \\ y &= 13 \end{aligned}$$

13.

$$7x - 30 = 5x + 14$$

$$\begin{array}{r} +30 \\ \hline 7x = 5x + 44 \\ -5x \quad -5x \\ \hline 2x = 44 \\ \frac{2x}{2} = \frac{44}{2} \\ \boxed{x = 22} \end{array}$$

$$3y + 11 + 124 = 180$$

$$3y + 135 = 180$$

$$\begin{array}{r} -135 \\ \hline 3y = 45 \\ \frac{3y}{3} = \frac{45}{3} \\ \boxed{y = 15} \end{array}$$

14.

$$23(7) = 161$$

$$23x - 16 + 8x - 21 = 180$$

$$31x - 37 = 180$$

$$\begin{array}{r} +37 \\ \hline 31x = 217 \\ \frac{31x}{31} = \frac{217}{31} \\ \boxed{x = 7} \end{array}$$

$$7y - 23 = 145$$

$$\begin{array}{r} +23 \\ \hline 7y = 168 \\ \boxed{y = 24} \end{array}$$

Topic 3: Proving Lines Are Parallel

For questions 17-18, find the value of x that would prove $j \parallel k$. State the converse that justifies your answer.

15.

$$14x - 25 = 129$$

$$\begin{array}{r} +25 \\ \hline 14x = 154 \\ \frac{14x}{14} = \frac{154}{14} \\ x = 11 \end{array}$$

Converse alt. int. converse

16.

$$2x - 8 + 9x - 10 = 180$$

$$11x - 18 = 180$$

$$\begin{array}{r} +18 \\ \hline 11x = 198 \\ x = 18 \end{array}$$

Converse SSI converse

Topic 4: Angles of Triangles

For questions 17-18, find the measure of each missing angle.

17.

$$64 + 81 = 145$$

$$180 - 145 = 35$$

$$m\angle 1 = 92$$

$$m\angle 2 = 24$$

$$m\angle 3 = 64$$

$$m\angle 4 = 35$$

$$m\angle 5 = 81$$

Triangle Sum
 $92 + 64 = 156$
 $180 - 156 = 24$

Angle Sum
 $35 + 64 = 99$
 $180 - 99 = 81$

18.

$$180 - 115 = 65$$

$$80 + 65 = 145$$

$$180 - 145 = 35$$

$$90 + 61 = 151$$

$$180 - 151 = 29$$

$$m\angle 1 = 35$$

$$m\angle 2 = 65$$

$$m\angle 3 = 29$$

$$m\angle 4 = 115$$

$$m\angle 5 = 65$$

$$m\angle 6 = 36$$

$$m\angle 7 = 144$$

For questions 19-20, find the $m\angle A$.

19.

$$9(11) + 17 = 116$$

$$3x - 4 + 9x + 17 + 6x - 31 = 180$$

$$18x - 18 = 180$$

$$\begin{array}{r} +18 \\ \hline 18x = 198 \\ x = 11 \end{array}$$

20.

$$115 + 29 = 144$$

$$180 - 144 = 36$$

$$5x - 27 + 7x - 26 = 10x - 23$$

$$12x - 53 = 10x - 23$$

$$\begin{array}{r} -10x \\ \hline 2x - 53 = -23 \\ +53 \quad +53 \\ \hline 2x = 30 \\ \frac{2x}{2} = \frac{30}{2} \\ \boxed{x = 15} \end{array}$$

Topic 5: Parallel and Perpendicular Lines

For questions 21-23, determine if AB and CD are parallel, perpendicular, or neither.

21. X_1, Y_1, X_2, Y_2 | X_1, Y_1, X_2, Y_2
 $A(-11, 5), B(-8, 4)$ | $C(8, -7), D(-1, -4)$

$$\frac{4-5}{-8-(-11)} = \frac{-1}{3} \quad \frac{-4-(-7)}{-1-8} = \frac{3}{-9} = -\frac{1}{3}$$

Slope of \overrightarrow{AB}	Slope of \overrightarrow{CD}	Types of Lines
$-\frac{1}{3}$	$-\frac{1}{3}$	parallel

22. X_1, Y_1, X_2, Y_2 | X_1, Y_1, X_2, Y_2
 $A(-3, 8), B(1, 15)$ | $C(10, -9), D(3, -5)$

$$\frac{15-8}{1-(-3)} = \frac{7}{4} \quad \frac{-5-(-9)}{3-10} = \frac{4}{-7}$$

Slope of \overrightarrow{AB}	Slope of \overrightarrow{CD}	Types of Lines
$\frac{7}{4}$	$-\frac{4}{7}$	perpendicular

23. X_1, Y_1, X_2, Y_2 | X_1, Y_1, X_2, Y_2
 $A(9, -3), B(9, 4)$ | $C(-2, 10), D(-2, 6)$

$$\frac{4-(-3)}{9-9} = \frac{7}{0} \quad \frac{6-10}{-2-(-2)} = \frac{-4}{0}$$

Slope of \overrightarrow{AB}	Slope of \overrightarrow{CD}	Types of Lines
undef.	undef.	parallel

For questions 24-25, determine if the lines are parallel, perpendicular, or neither.

24. $6x + 10y = 20$ and $5x - 3y = 21$

$$\frac{10y}{10} = \frac{-6x+20}{10} \quad \frac{-3y}{-3} = \frac{-5x+21}{-3}$$

$$y = -\frac{3}{5}x + 2 \quad y = \frac{5}{3}x - 7$$

$m = -3/5$ $m = 5/3$

perpendicular

25. $x - y = 4$ and $x + y = 9$

$$\frac{-y}{-1} = \frac{-x+4}{-1} \quad y = -x + 9$$

$$y = x - 4 \quad m = 1$$

$$m = -1$$

perpendicular